A Generalization of Weinstein's Morphism

Andrés Pedroza

In 1989, A. Weinstein introduced a morphism

$$A: \pi_1(\operatorname{Ham}(M, \omega)) \to \mathbb{R}/\mathcal{P}_2(M, \omega),$$

defined via the action functional of Hamiltonian diffeomorphisms. Here, $\operatorname{Ham}(M,\omega)$ denotes the group of Hamiltonian diffeomorphisms of the symplectic manifold (M,ω) .

In this talk, we present a generalization of Weinstein's morphism to higher homotopy groups:

$$A: \pi_{2k-1}(\operatorname{Ham}(M,\omega)) \to \mathbb{R}/\mathcal{P}_{2k}(M,\omega),$$

for all $1 \leq k \leq n$. As an application, we show that the groups $\pi_{2k-1}(\operatorname{Ham}(\widetilde{\mathbb{C}P}^n,\widetilde{\omega}_\rho))$ contain an element of infinite order.